

Running Head: ORGANIC CHEMISTRY

Organic Chemistry

Q1: Derive an equation describing the relationship between the G-value of polymer mean chain length and the dose-rate.

Q2: For radiation-induced polymerization (at high degree of polymerization and at steady state radiolysis), derive an equation by which you can demonstrate that the overall rate of polymerization depends on the monomer concentration  $[M]$ , monomer radical concentration, and the radical concentration produced from the solvent.

Q3: In the pulse radiolysis of  $N_2O$ -saturated aqueous solutions of  $[0.9 \times 10^{-2} M]$  poly vinyl pyrrolidone (with  $M_{w,0} = 360,000 \text{ g/mol}$ ), it was found that the concentration of the number of inter-molecular crosslinking bonds in a unit volume of sample is  $2 \times 10^{-7} \text{ ML}^{-1}$ . Determine the  $M_w$  of the poly vinyl pyrrolidone, and the  $G(\text{crosslinking})$  assuming that the solution was received 5 kGy of dose.

Q4: A polymer with weight average degree of polymerization ( $M_w$ ) (assuming random distribution) of  $10^5$  and the minimum required absorbed dose for gel formation ( $r_g$ ) is 30 kGy. Calculate the values for crosslinks and crosslinks units in **SI** units (mole per joule) and what are the values of the weight average molecular weight after irradiation and  $\gamma$ ?

Q5: During the radiolysis of polyethylene, the following results were generated:

D (MGy)	Sol fraction (s)
0.250	0.788
0.200	0.932
0.167	1.07
0.143	1.16
0.125	1.25

Calculate the  $G$  (scission), assuming the  $G$  (crosslink) = 1.16 per 100 eV.

Q6: How many crosslinks per weight average and number average polymer molecule are required to reach the gel point

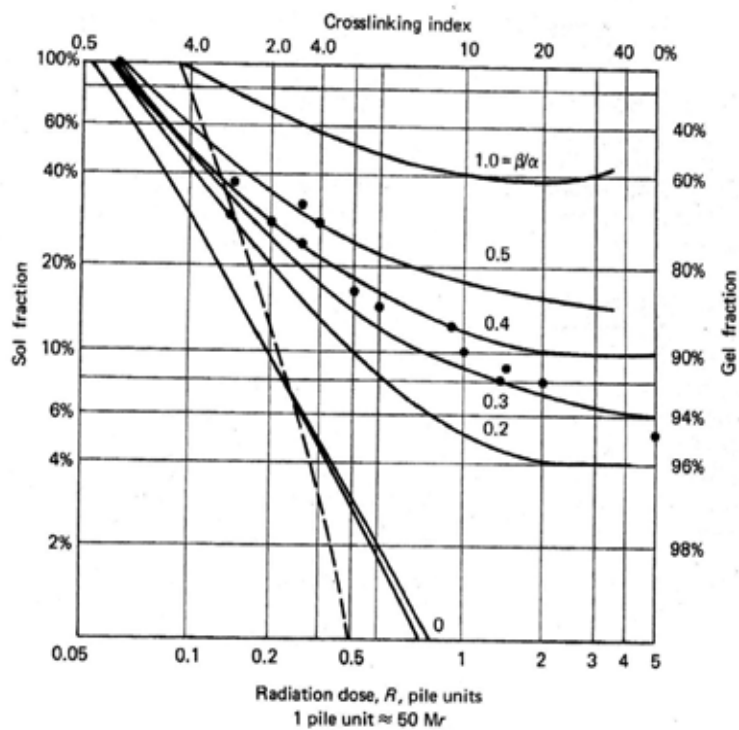
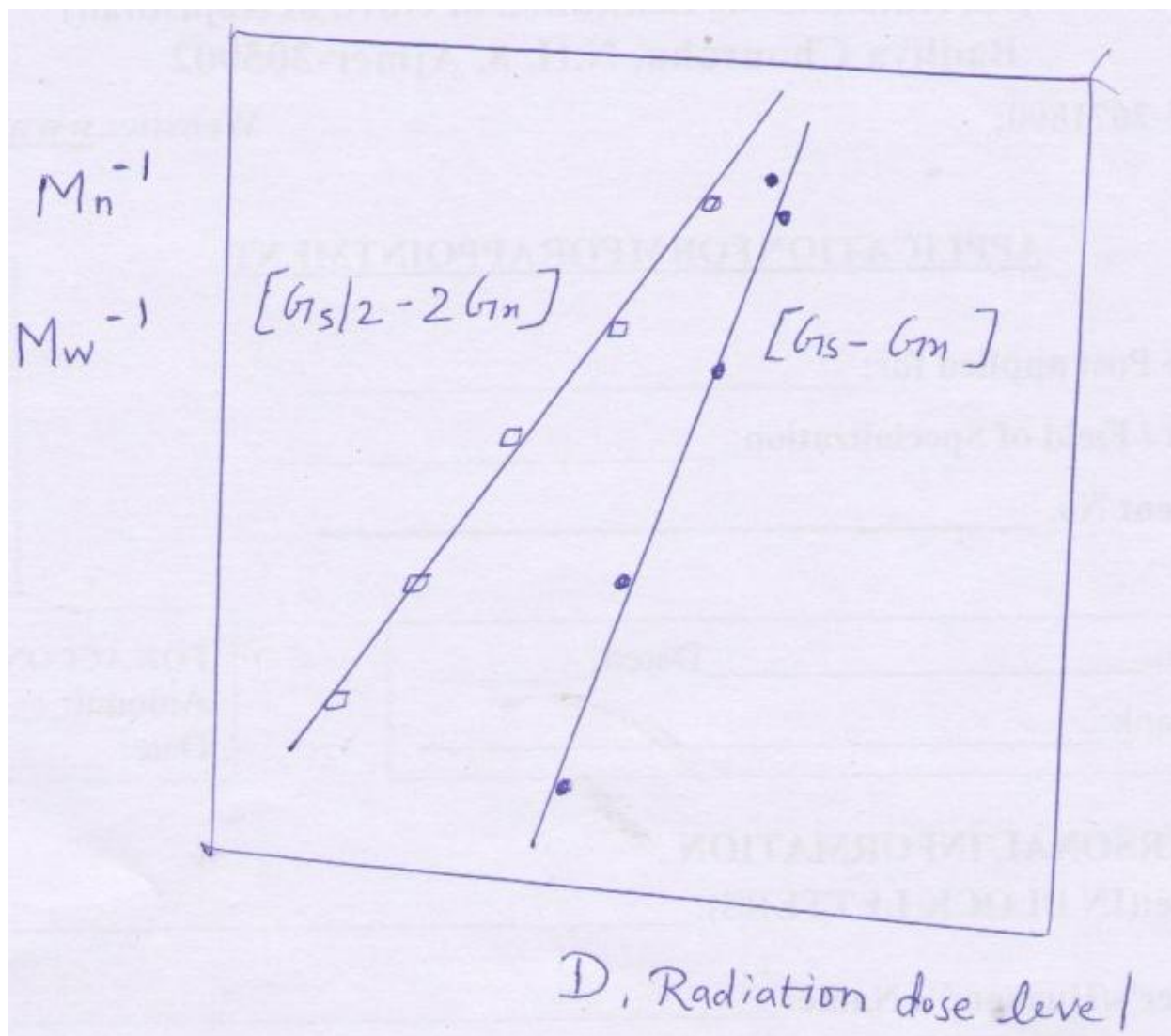


Fig. . . Sol and gel fraction of irradiated polyethylene. The black dots indicate observed values, solid lines indicate theoretical curve assuming a random probability initially (numbers represent ratio of chain fracture to crosslinking), and broken lines indicate theoretical curve assuming uniform initial distribution (no chain fracture). (A. Charlesby, "Atomic Radiation and Polymers," Pergamon Press, London, 1960.)

Q7: Develop an equation for the degree of polymerization at high dose-rates.

## Answer-1



Relation Between  $G$ -value of Polymer mean chain length and dose Rate

$$M_n^{-1} = M_{n,0}^{-1} + [G_s - G_m] D / 100 N_{av}$$

$$M_w^{-1} = M_{w,0}^{-1} + [G_s / 2 - 2 G_m] D / 100 N_{av}$$

$$G_s = G_{scission}$$

$$D = \text{Dose level}$$

$$M_w = \text{Molecular weight}$$

$$G_m = \text{Crosslinking}$$

### Answer-2

In polymerization, the reaction rate for initiation, propagation and termination is defined in following manner.

$$v_i = d[M\cdot]/dt = 2k_d f [I]$$

$$v_p = k_p [M][M\cdot]$$

$$v_t = -d[M\cdot]/dt = 2k_t [M\cdot]^2$$

In this,  $f$  is denoted as the efficiency of the initiator and  $k_d$ ,  $k_p$ , and  $k_t$  are defined as the constants for three phases of polymerization those are initiator dissociation, chain propagation and termination.  $[I]$ ,  $[M]$  and  $[M\cdot]$  is the concentration of the initiator, monomer and the active growing chain. In the steady rate approximation, the concentration of the active growing

chains remains constant, like, the rate of initiation and termination is identical. The concentration of active chain can be deduced and conveyed in some known species (Sorrell, 2006).

$$[M\cdot] = \left(\frac{k_d[I]f}{k_t}\right)^{1/2}$$

Under this case, the rate of chain propagation can be defined with the use of a function of the initiator and monomer concentration

$$rate = k_p \left(\frac{fk_d}{k_t}\right)^{1/2} [I]^{1/2} [M]$$

The kinetic chain length  $v$  is a aspect of the standard item of monomer units those react with an active center in the period of its life time and is linked to the molecular weight with the termination mechanism (Sorrell, 2006). The dynamic chain length is the function of propagation rate and initiation rate, without chain transfer,

$$v = \frac{R_p}{R_d} = \frac{k_p[M][M\cdot]}{2fk_d[I]} = \frac{k_p[M]}{2(fk_dk_t[I])^{1/2}}$$

With lack of chain transfer effect occurs in the reaction,  $P_n$ , the number average degree of polymerization can be associated with the length of the kinetic chain. 1 polymer molecule is developed per every kinetic chain under the termination by disproportionation,

$$P_n = v$$

Termination by combination results in the production of one polymer molecule per two kinetic chains:

$$P_n = 2v$$

Any mixture of these both mechanisms can be described by using the value  $\delta$ , and the contribution of disproportionation to the overall termination process:

$$P_n = \frac{2}{1 + \delta} v$$

If chain transfer is taken into consideration, then there are some other methods to conclude the growing chain. The equation for dynamic chain length will be modified as the following.

If chain transfer is taken into consideration, the kinetic chain length is not influenced by the transfer process, as the growing free-radical center produced by the initiation step stays energetic after any event of chain transfer, even though multiple polymer chains are produced. Nevertheless, the number average degree of polymerization reduces as the chain transfers, since the developing chains are finished by the events of chain transfer (Sorrell, 2006). By considering the chain transfer reaction towards solvent  $S$ , initiator  $I$ , polymer  $P$ , and added chain transfer agent  $T$ , the  $P_n$  equation can be enhanced:

$$\frac{1}{P_n} = \frac{2k_{t,d} + k_{t,c}}{k_p^2 [M]^2} R_p + C_M + C_S \frac{[S]}{[M]} + C_I \frac{[I]}{[M]} + C_P \frac{[P]}{[M]} + C_T \frac{[T]}{[M]}$$

It is usual to define chain transfer constants  $C$  for the different molecules

$$C_M = \frac{k_{tr}^M}{k_p}, \quad C_S = \frac{k_{tr}^S}{k_p}, \quad C_I = \frac{k_{tr}^I}{k_p}, \quad C_P = \frac{k_{tr}^P}{k_p}, \quad C_T = \frac{k_{tr}^T}{k_p}$$

Answer 3 . $M_w = 360,000\text{g/mol}$

$$\text{cross linking bond} = 2 \times 10^{-7} \text{ mc}^{-1}$$

D = 5 kGy of dose

$$M_w^{-1} = M_w^{-1}{}_0 + (Gs/2 - 2 Gx) / D/100 \text{ Nav}$$

$$M_w^{-1} = 360000 + (2 \times 10^{-7} - 2 \times 0.9 \times 10^{-2}) / 5/100 \text{ Nav}$$

$$M_w^{-1} = 360000 + (2 \times 10^{-7} - 1.8 \times 10^{-2}) / 20 \text{ Nav}$$

$$M_w^{-1} = 360000 + (0.2 \times 10^{-5}) / 0.05$$

$$M_w^{-1} = 360000 + 0.01 \times 10^{-5}$$

$$M_w^{-1} = 360000.01 \times 10^{-5}$$

$$M_w = 360000.01 \times 10^{-4}$$

Now calculate G

$$D_{\text{gel}} = 0.5 \times 10^7 / G(x) M_w$$

$$D = 5 \text{ kGy}$$

$$M_w = 360000.01 \times 10^{-4}$$

Now G = ?

$$5 = 0.5 \times 10^7 / G(x) \times 360000.01 \times 10^{-4}$$

$$Gx = 0.5 \times 10^7 / 5 \times 360000.01 \times 10^{-4}$$

$$Gx = 0.5 \times 10^7 / 1800000.05 \times 10^{-4}$$

$$Gx = 36000001 \times 10^3$$

#### Answer-4

Ans 4. calculate G (crosslink)

$$D_{\text{gel}} = 0.5 \times 10^7 / G(x) \text{ Mw}$$

$$D = 30 \text{ kGy}$$

$$\text{Mw} = 1 \times 10^5$$

$$\text{Now } G = 0.5 \times 10^7 / D_{\text{gel}} \times \text{Mw}$$

$$G = 0.5 \times 10^7 / 30 \times 1 \times 10^5$$

$$G = 0.5 \times 10^7 / 30 \times 10^5$$

$$G = 0.0166 \times 10^2 \text{ mole per joule}$$

$$\text{In SI unit } G = 0.0166 \times 10^2 \text{ m}^2 \cdot \text{kg} \cdot \text{s}^{-2} \cdot \text{mol}^{-1}$$

### Answer-5

Calculate  $G_{\text{scission}}$

$$M_n^{-1} = M_n^{-1} \text{ }_0 + (G_s - G_x) D / 100 N_{\text{av}}$$

$G_{\text{value}}$  = no. of events (yield) per 100eV or radiation energy

$$100 \text{ eV} = 1.602 \times 10^{-17} \text{ kGy.g}$$

$$M_n^{-1} = M_n^{-1} \text{ }_0 + (G_s - G_x) D / 100 N_{\text{av}}$$

$$M_n^{-1} = \text{no. of radiolysis} = 5$$

$$G_s = G_{\text{scission}} = ?$$

$$G_x = G_{\text{crosslink}} = 1.16 \text{ per } 100 \text{ eV.}$$

$$100 \text{ eV} = 1.602 \times 10^{-17} \text{ kGy.g}$$

$$\text{So } G_x = 1.16 \times 1.602 \times 10^{-17} \text{ kgy.g}$$

$$= 1.85832 \times 10^{-17} \text{ kGy.g}$$

D (MGy)	Sol fraction (s)
0.250	0.788
0.200	0.932
0.167	1.07
0.143	1.16
0.125	1.25

$$D = 0.250 + 0.200 + 0.167 + 0.143 + 0.125 = 0.885/5 = 0.177$$

$$Mn^{-1} = Mn^{-1} 0 + (Gs - Gx) D/100 Nav$$

$$5 = 5 + (Gs - 1.85832 \times 10^{-17}) 0.177/100$$

$$Gs = 5 + (-1.85832 \times 10^{-17}/5) 0.00177$$

$$Gs = 5 + (0.07433 \times 10^{-17}) 0.00177$$

$$Gs = 5 + 0.000131 \times 10^{-17} = Gs = 5.000131 \times 10^{-17}$$

### Answer-6

$$ANS.6 Pc = 1 / (R + Rp(F-2))0.5$$

$$R = \text{RADIATION DOSE PILE UNIT 1 PILE UNIT} = 50\text{mr}$$

$$\text{In this graph gel point is 5 so } r = 5 \times 50 = 250$$

$$P = 0.2$$

$$F = 96\%$$

$$Pc = 1 / (250 + 250 \times 0.2 (96/100 - 2)) 0.5$$

$$= 1 / 250 + 50 (0.96 - 2) 0.5$$

$$= 1/300 (1.04) 0.5$$

$$= 1/300 \times 0.52$$

$$= 1/156.00$$

$$= 0.00641 = 64 \times 10^{-4} \text{ m}^2 \cdot \text{kg} \cdot \text{s}^{-2} \cdot \text{mol}^{-1} \text{ crosslinks are required}$$

### References

Sorrell, T.N. (2006). *Organic chemistry*. University Science Books.

United States Application US20100029884 (2010). Retrieved December, 18 2010 from

<http://www.freepatentsonline.com/20100029884.pdf>

